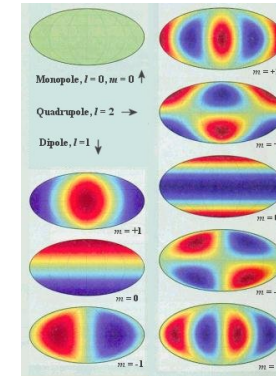
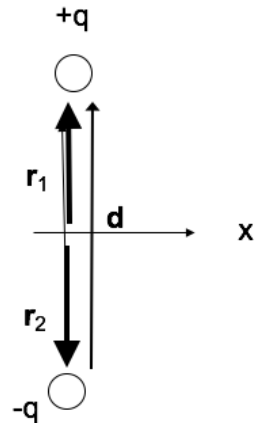


# MULTIPOLE EXPANSION

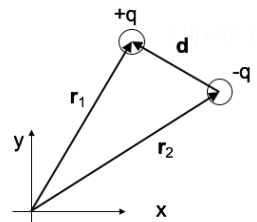


Multipole Expansion of the Power Spectrum of CMBR



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the value of the dipole moment?  $\sum_i q_i \mathbf{r}_i$

- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the dipole moment of this configuration?

$$\sum_i q_i \mathbf{r}_i$$

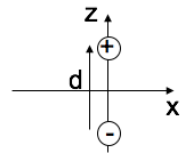
- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

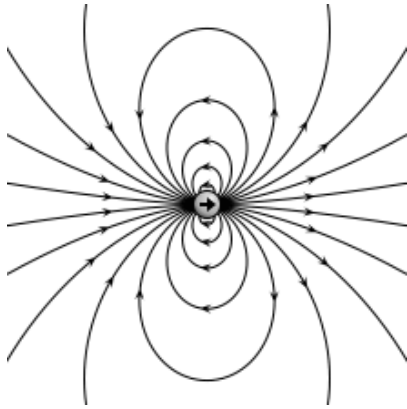
$$\mathbf{E}_{dip}(\mathbf{r}) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

For the dipole  $\mathbf{p} = q\mathbf{d}$  shown, what does the formula predict for the direction of  $\mathbf{E}(\mathbf{r} = 0)$ ?

- A. Down
- B. Up
- C. Some other direction
- D. The formula doesn't apply



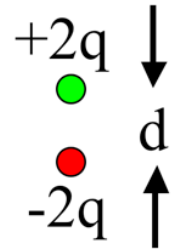
## IDEAL VS. REAL DIPOLE



$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the magnitude of the dipole moment of this charge distribution?

- A.  $qd$
- B.  $2qd$
- C.  $3qd$
- D.  $4qd$
- E. It's not determined



$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the dipole moment of this system?

(BTW, it is NOT overall neutral!)

- A.  $q\mathbf{d}$
- B.  $2q\mathbf{d}$
- C.  $\frac{3}{2}q\mathbf{d}$
- D.  $3q\mathbf{d}$
- E. Something else (or not defined)

