

You are trying to compute the work done by a force, $\mathbf{F} = a\hat{x} + x\hat{y}$, along the line $y = 2x$ from $\langle 0, 0 \rangle$ to $\langle 1, 2 \rangle$.

What is $d\mathbf{l}$?

- A. dl
- B. $dx \hat{x}$
- C. $dy \hat{y}$
- D. $2dx \hat{x}$
- E. Something else

You are trying to compute the work done by a force, $\mathbf{F} = a\hat{x} + x\hat{y}$, along the line $y = 2x$ from $\langle 0, 0 \rangle$ to $\langle 1, 2 \rangle$. Given that $d\mathbf{l} = dx \hat{x} + dy \hat{y}$, which of the following forms of the integral is correct?

- A. $\int_0^1 a dx + \int_0^2 x dy$
- B. $\int_0^1 (a dx + 2x dx)$
- C. $\frac{1}{2} \int_0^2 (a dy + y dy)$
- D. More than one is correct

A certain fluid has a velocity field given by $\mathbf{v} = x\hat{x} + z\hat{y}$. Which component(s) of the field contributed to "fluid flux" integral $(\int_S \mathbf{v} \cdot d\mathbf{A})$ through the x-z plane?

- A. v_x
- B. v_y
- C. both
- D. neither

For the same fluid with velocity field given by $\mathbf{v} = x\hat{x} + z\hat{y}$. What is the value of the "fluid flux" integral $(\int_S \mathbf{v} \cdot d\mathbf{A})$ through the entire x-y plane?

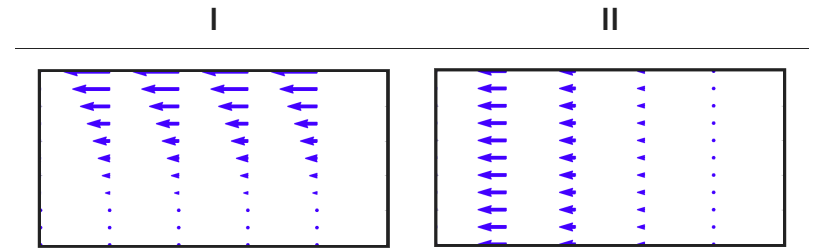
- A. It is zero
- B. It is something finite
- C. It is infinite
- D. I can't tell without doing the integral

A rod (radius R) with a hole (radius r) drilled down its entire length L has a mass density of $\frac{\rho_0\phi}{\phi_0}$ (where ϕ is the normal polar coordinate).

To find the total mass of this rod, which coordinate system should be used (take note that the mass density varies as a function of angle):

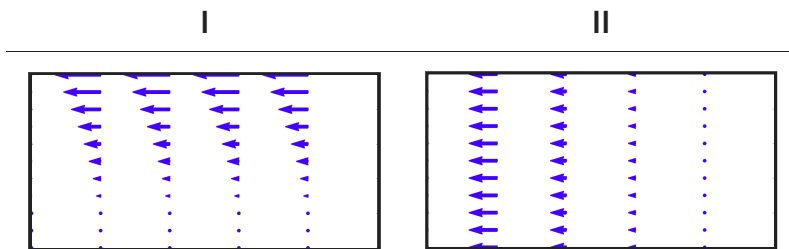
- A. Cartesian (x, y, z)
- B. Spherical (r, ϕ, θ)
- C. Cylindrical (s, ϕ, z)
- D. It doesn't matter, just pick one.

Which of the following two fields has zero divergence?



- A. Both do.
- B. Only I is zero
- C. Only II is zero
- D. Neither is zero
- E. ???

Which of the following two fields has zero curl?



- A. Both do.
- B. Only I is zero
- C. Only II is zero
- D. Neither is zero
- E. ???

Consider a vector field defined as the gradient of some well-behaved scalar function:

$$\mathbf{v}(x, y, z) = \nabla T(x, y, z).$$

What is the value of $\oint_C \mathbf{v} \cdot d\mathbf{l}$?

- A. Zero
- B. Non-zero, but finite
- C. Can't tell without a function for T