Consider a solid sphere of charge that has a charge density that varies with $\cos \theta$. What can we say about the terms in the general solution to Laplace's equation outside there sphere?

$$
V(r, \theta)=\sum_{l}\left(A_{l} r^{l}+\frac{B_{l}}{r^{(l+1)}}\right) P_{l}(\cos \theta)
$$

A. All the $A_{l}$ 's are zero
B. All the $B_{l}$ 's are zero
C. Only $A_{0}$ should remain
D. Only $B_{0}$ should remain
E. Something else

Two charges are positioned as shown to the left. The relative position vector between them is $\mathbf{d}$. What is the value of of the dipole moment? $\sum_{i} q_{i} \mathbf{r}_{i}$

A. $+q \mathbf{d}$<br>B. $-q \mathbf{d}$<br>C. Zero<br>D. None of these

## MULTIPOLE EXPANSION



Multipole Expansion of the Power Spectrum of CMBR

Two charges are positioned as shown to the left. The relative position vector between them is $\mathbf{d}$. What is the dipole moment of this configuration?

$$
\sum_{i} q_{i} \mathbf{r}_{i}
$$

A. $+q \mathbf{d}$
B. $-q \mathbf{d}$
C. Zero
D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

$$
\mathbf{E}_{d i p}(\mathbf{r})=\frac{p}{4 \pi \varepsilon_{0} r^{3}}(2 \cos \theta \hat{\mathbf{r}}+\sin \theta \hat{\theta})
$$

For the dipole $\mathbf{p}=q \mathbf{d}$ shown, what does the formula predict for the direction of $\mathbf{E}(\mathbf{r}=0)$ ?
A. Down
B. Up

C. Some other direction
D. The formula doesn't apply

## IDEAL VS. REAL DIPOLE



