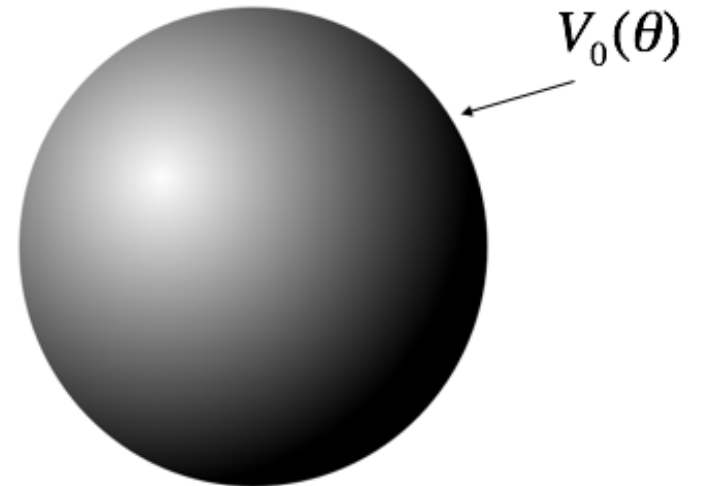


How many boundary conditions (on the potential  $V$ ) do you use to find  $V$  inside the spherical plastic shell?

- A. 1
- B. 2
- C. 3
- D. 4
- E. It depends on  $V_0(\theta)$



$$V(r, \theta) = \sum_{l=0}^{\infty} \left( A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \theta)$$

Suppose  $V$  on a spherical shell is:

$$V(R, \theta) = V_0 (1 + \cos^2 \theta)$$

Which terms do you expect to appear when finding  **$V(\text{inside})$** ?

- A. Many  $A_l$  terms (but no  $B_l$ 's)
- B. Many  $B_l$  terms (but no  $A_l$ 's)
- C. Just  $A_0$  and  $A_2$
- D. Just  $B_0$  and  $B_2$
- E. Something else!

$$V(r, \theta) = \sum_{l=0}^{\infty} \left( A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \theta)$$

Suppose  $V$  on a spherical shell is:

$$V(R, \theta) = V_0 (1 + \cos^2 \theta)$$

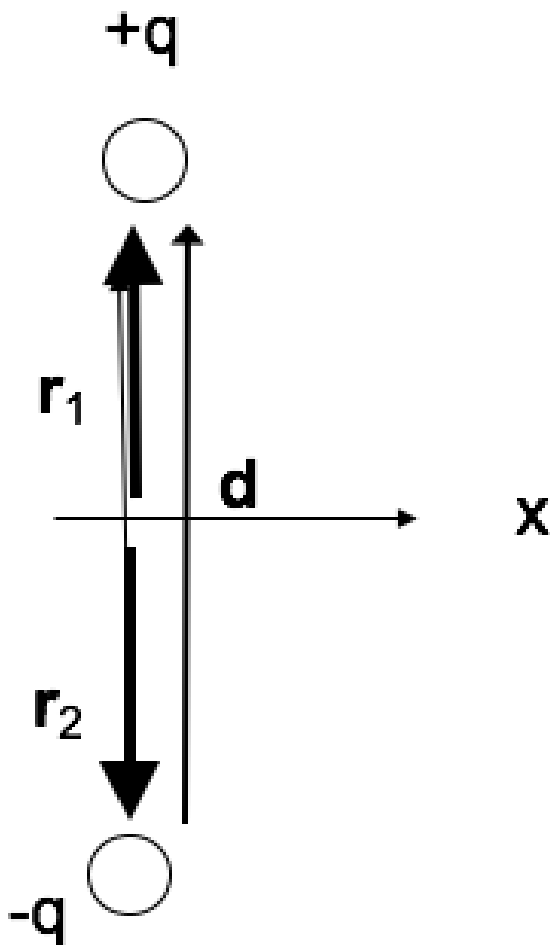
Which terms do you expect to appear when finding  **$V(\text{outside})$** ?

- A. Many  $A_l$  terms (but no  $B_l$ 's)
- B. Many  $B_l$  terms (but no  $A_l$ 's)
- C. Just  $A_0$  and  $A_2$
- D. Just  $B_0$  and  $B_2$
- E. Something else!

Consider a solid sphere of charge that has a charge density that varies with  $\cos \theta$ . What can we say about the terms in the general solution to Laplace's equation outside there sphere?

$$V(r, \theta) = \sum_l \left( A_l r^l + \frac{B_l}{r^{(l+1)}} \right) P_l(\cos \theta)$$

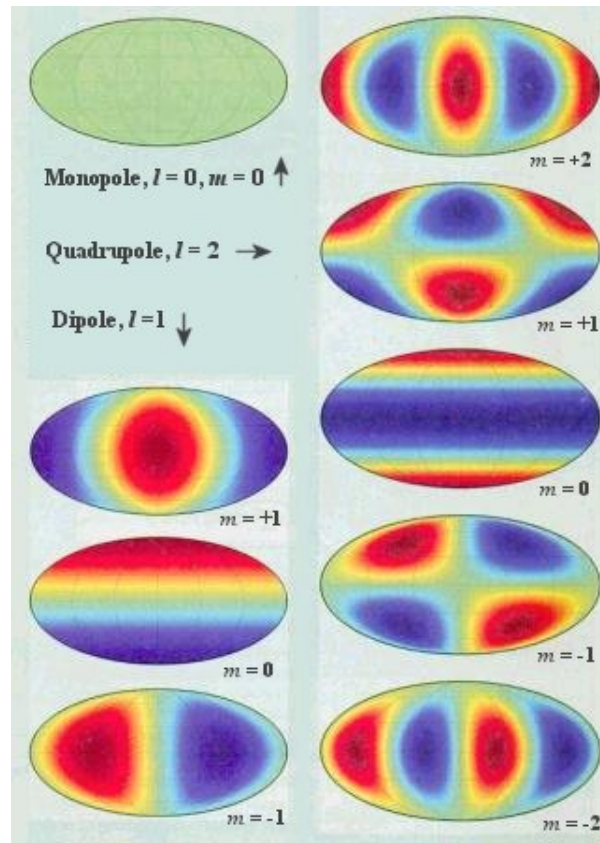
- A. All the  $A_l$ 's are zero
- B. All the  $B_l$ 's are zero
- C. Only  $A_0$  should remain
- D. Only  $B_0$  should remain
- E. Something else



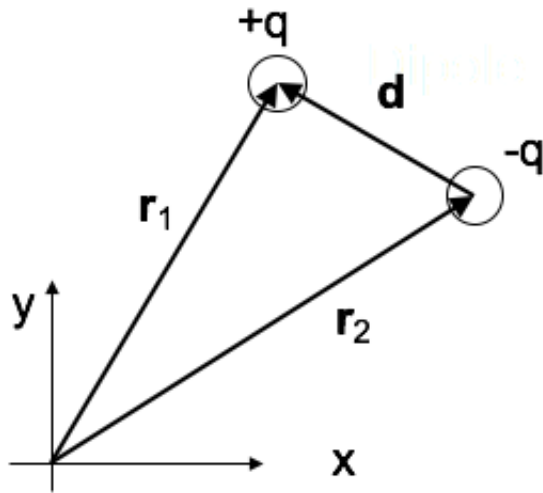
Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the value of the dipole moment?  $\sum_i q_i \mathbf{r}_i$

- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these

# MULTIPOLE EXPANSION



Multipole Expansion of the Power Spectrum of CMBR



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the dipole moment of this configuration?

$$\sum_i q_i \mathbf{r}_i$$

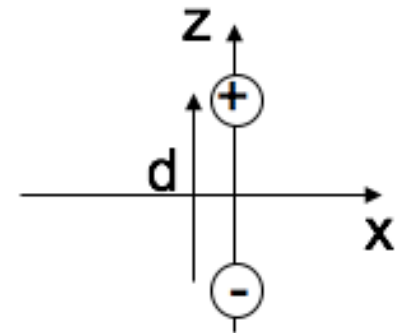
- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

$$\mathbf{E}_{dip}(\mathbf{r}) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

For the dipole  $\mathbf{p} = q\mathbf{d}$  shown, what does the formula predict for the direction of  $\mathbf{E}(\mathbf{r} = 0)$ ?

- A. Down
- B. Up
- C. Some other direction
- D. The formula doesn't apply





# IDEAL VS. REAL DIPOLE

