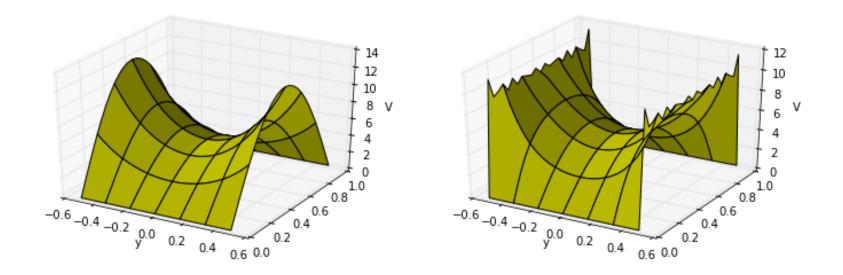
What is the value of  $\int_0^a \sin(n\pi x/a) \sin(m\pi x/a) dx$ ? A. Zero B. Non-zero C. Depends on *n* and *m* 

## **EXACT SOLUTIONS:**

$$V(x, y) = \sum_{n=1}^{\infty} \frac{4V_0}{n\pi} \frac{1}{\cosh\left(\frac{n\pi}{2}\right)} \cosh\left(\frac{n\pi x}{a}\right) \sin\left(\frac{n\pi y}{a}\right)$$

## APPROXIMATE SOLUTIONS: (1 TERM; 20 TERMS)



Given that we want to solve Laplace's equation in 2D and that we have a description for the numerical second derivative of one variable,

$$f''(x) \approx \frac{f(x+a) - 2f(x) + f(x-a)}{a^2}$$

what is the appropriate numerical partial derivative for  $V(x, y), \partial^2 V/\partial x^2 \approx$ ,

A.  $[V(x + a) - 2V(x) + V(x - a)]/a^2$ B.  $[V(x + a, y) - 2V(x, y) + V(x - a, y)]/a^2$ C.  $[V(y + a) - 2V(y) + V(y - a)]/a^2$ D.  $[V(x, y + a) - 2V(x, y) + V(x, y - a)]/a^2$ E. More than one is correct Given that the potential at any point is given by the average of the surrounding points,

$$V(x, y) \approx \frac{1}{4} [V(x + a, y) + V(x, y + a) + V(x - a, y) + V(x, y - a)]$$

Draft the psuedocode for finding the approximate potential.

Given  $\nabla^2 V = 0$  in Cartesian coords, we separated V(x, y, z) = X(x)Y(y)Z(z). Will this approach work in spherical coordinates, i.e. can we separate  $V(r, \theta, \phi) = R(r)\Theta(\theta)\Phi(\phi)$ ?

A. Sure.

- B. Not quite the angular components cannot be isolated, e.g.,  $f(r, \theta, \phi) = R(r)Y(\theta, \phi)$
- C. It won't work at all because the spherical form of Laplace's Equation has cross terms in it (see the front cover of Griffiths)

## **SEPARATION OF VARIABLES (SPHERICAL)**

