

I have seen Separation of Variables before.

- A. Yes, and I'm comfortable with it.
- B. Yes, but I don't quite remember.
- C. Nope
- D. I'm triggered.

Say you have three functions $f(x)$, $g(y)$, and $h(z)$. $f(x)$ depends on x but not on y or z . $g(y)$ depends on y but not on x or z . $h(z)$ depends on z but not on x or y .

If $f(x) + g(y) + h(z) = 0$ for all x, y, z , then:

- A. All three functions are constants (i.e. they do not depend on x, y, z at all.)
- B. At least one of these functions has to be zero everywhere.
- C. All of these functions have to be zero everywhere.
- D. All three functions have to be linear functions in x, y , or z respectively (such as $f(x) = ax + b$)

If our general solution contains the function,

$$X(x) = Ae^{\sqrt{c}x} + Be^{-\sqrt{c}x}$$

What does our solution look like if $c < 0$; what about if $c > 0$?

- A. Exponential; Sinusoidal
- B. Sinusoidal; Exponential
- C. Both Exponential
- D. Both Sinusoidal
- E. ???

Our example problem has the following boundary conditions:

- $V(0, y > 0) = 0; V(a, y > 0) = 0$
- $V(x_{0 \rightarrow a}, y = 0) = V_0; V(x, y \rightarrow \infty) = 0$

If $X'' = c_1 X$ and $Y'' = c_2 Y$ with $c_1 + c_2 = 0$, which is constant is positive?

A. c_1

B. c_2

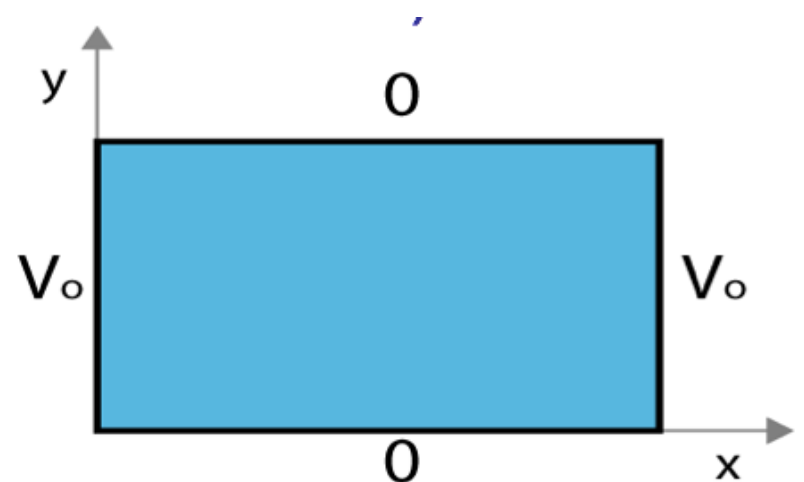
C. It doesn't matter either can be

Given the two diff. eq's :

$$\frac{1}{X} \frac{d^2 X}{dx^2} = C_1 \quad \frac{1}{Y} \frac{d^2 Y}{dy^2} = C_2$$

where $C_1 + C_2 = 0$. Given the boundary conditions in the figure, which coordinate should be assigned to the negative constant (and thus the sinusoidal solutions)?

- A. x
- B. y
- C. $C_1 = C_2 = 0$ here
- D. It doesn't matter.

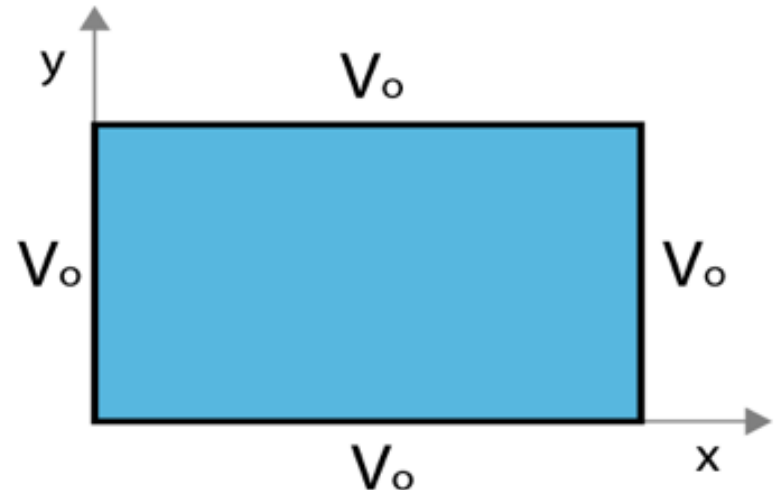


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- D. It doesn't matter.



When does $\sin(ka)e^{-ky}$ vanish?

A. $k = 0$

B. $k = \pi/(2a)$

C. $k = \pi/a$

D. A and C

E. A, B, C

Suppose $V_1(r)$ and $V_2(r)$ are linearly independent functions which both solve Laplace's equation, $\nabla^2 V = 0$.

Does $aV_1(r) + bV_2(r)$ also solve it (with a and b constants)?

- A. Yes. The Laplacian is a linear operator
- B. No. The uniqueness theorem says this scenario is impossible, there are never two independent solutions!
- C. It is a definite yes or no, but the reasons given above just aren't right!
- D. It depends...