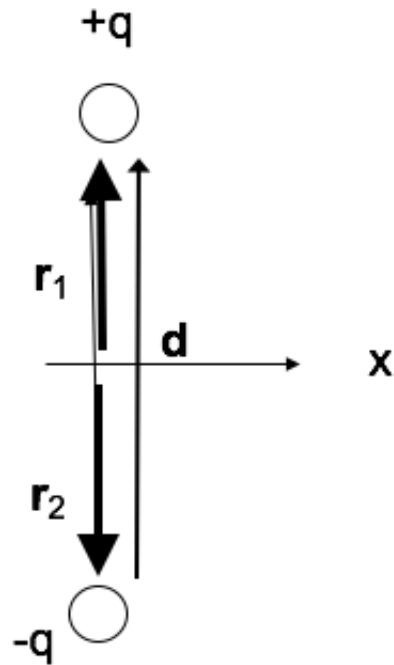


Consider a solid sphere of charge that has a charge density that varies with  $\cos \theta$ . What can we say about the terms in the general solution to Laplace's equation outside there sphere?

$$V(r, \theta) = \sum_l \left( A_l r^l + \frac{B_l}{r^{(l+1)}} \right) P_l(\cos \theta)$$

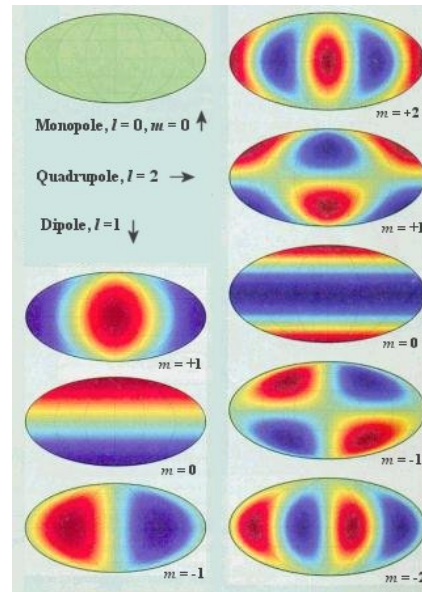
- A. All the  $A_l$ 's are zero
- B. All the  $B_l$ 's are zero
- C. Only  $A_0$  should remain
- D. Only  $B_0$  should remain
- E. Something else



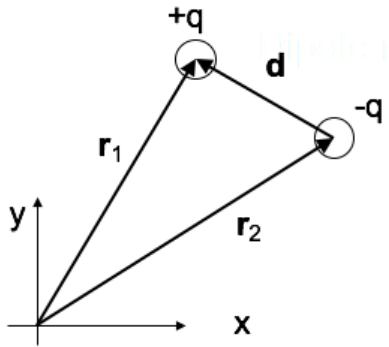
Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the value of the dipole moment?  $\sum_i q_i \mathbf{r}_i$

- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these

# MULTIPOLE EXPANSION



Multipole Expansion of the Power Spectrum of CMBR



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the dipole moment of this configuration?

$$\sum_i q_i \mathbf{r}_i$$

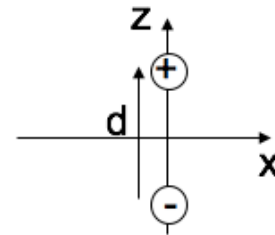
- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

$$\mathbf{E}_{dip}(\mathbf{r}) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

For the dipole  $\mathbf{p} = q\mathbf{d}$  shown, what does the formula predict for the direction of  $\mathbf{E}(\mathbf{r} = 0)$ ?

- A. Down
- B. Up
- C. Some other direction
- D. The formula doesn't apply



# IDEAL VS. REAL DIPOLE

